
How to Choose a Threshold for the LLM Evaluation Metrics

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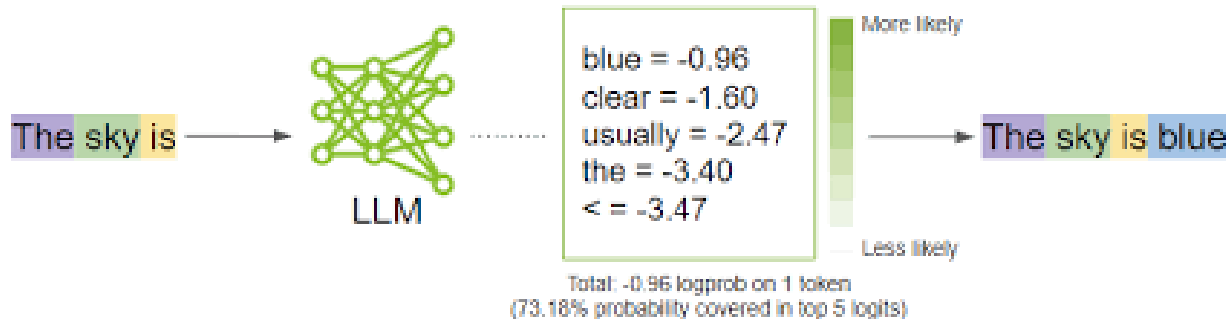
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<https://arxiv.org/abs/2412.12148>

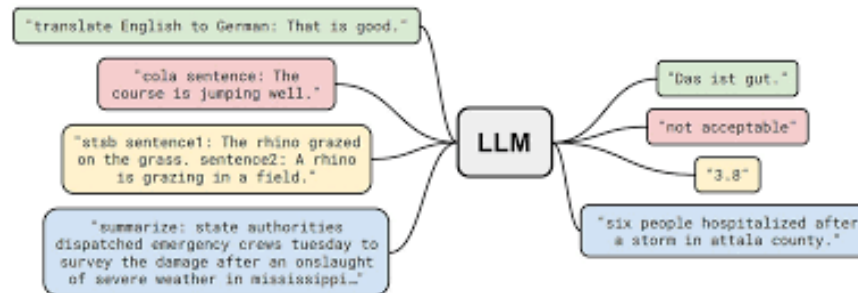
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Large Language Models (LLMs)

- An LLM is a GenAI algorithm which though trained in a supervised fashion (next word prediction, it learns the joint distribution of the given large corpus of text data.



- Once trained, it can be used for many different down-stream tasks not just next word prediction.



- Usually, an LLM is trained with massive computational efforts. Most non-tech companies may not have resources to train LLMs from scratch (...yet!).
- Hence, most companies rely on third-party pre-trained, i.e., foundation models such as Llama-3 (Meta), GPTs (OpenAI), Gemini (Google), Claude (Anthropic), etc.

Retrieval Augmented Generation: where can things go wrong

Input Query/Prompt

- Toxicity
- Prompt Injection
- Personal Identifier Information
- Prompt Injection/Jailbreak/Adversarial attacks
- Off-topic (e.g., medical advice)
- Domain specific legally or otherwise prohibited queries (e.g., investment advice)

Output/Answer

- Toxicity
- Personal Identifier Information
- Copyrighted information
- Incorrect/irrelevant answers
- Domain specific legally or otherwise prohibited queries (e.g., investment advice)
- Bias/Fairness (e.g., information about muni assets having bias for 'Blue' vs 'Red' states)
- Explainability
- Uncertainty quantification

Retrieval Augmented Generation: Objective Evaluation Metrics

- There are numerous evaluation metrics for the LLM systems (e.g., RAG or text summarization, etc.) proposed in the literature.
- They can be broadly classified into two categories:
 1. 'Offline' evaluation metrics: they require ground truth QA pairs and/or context.
 - These evaluation metrics are useful to validate an LLM system in an 'off-line mode'.
 - e.g., answer similarity metrics (Euclidean distance, longest common sequence, Bleu, Rouge, BERTScore, etc.)
 2. 'Online' evaluation metrics: they do not require ground truth Q&A pairs or context.
 - These evaluation metrics are useful to continuously monitor the LLM application system when it is online and we cannot have ground truths any more.
 - e.g., Groundedness/Faithfulness, Diversity, Coherence, etc.

A Concrete Example: Groundedness/Faithfulness

- **Is the answer supported by the context?**
- For a given query, q , the answer, $as(q)$, is faithful to the context, $c(q)$, if the claims that are made in the answer can be inferred from the context.
- To estimate faithfulness, we first use an LLM to extract a set of statements, i.e., decompose longer sentences in the answer into shorter and more focused assertions.
- For each statement, s_i , the LLM determines if s_i can be inferred from $c(q)$. Prompt (RAGAS):

Given a question and answer, create one or more statements from each sentence in the given answer.

Question: "{question}"

Answer: "{answer}"

Consider the given context and following statements, then determine whether they are supported by the information present in the context. Provide a brief explanation for each statement before arriving at the verdict (Yes/No). Provide a final verdict for each statement in order at the end in the given format. Do not deviate from the specified format.

Context: "{context}"

- Then, Faithfulness = (No. of verified sentences)/(Total no. of sentences in the answer)

Retrieval Augmented Generation: Groundedness/Faithfulness

- **Is the answer supported by the context?**

E.g.,

question = "What is the capital of France?"

context = "The capital of France is Paris. Paris is known for its culture, history, and landmarks such as the Eiffel Tower."

answer = "The capital of France is Paris. It is a large city with a significant cultural heritage."

- Generated statements from the :
 1. Paris is the capital of France.
 2. Paris is a city with a rich cultural heritage.
 3. The Eiffel Tower is a landmark in Paris.
- Explanations:
 1. The first statement is directly supported by the context, which states that "The capital of France is Paris.". Verdict: Yes
 2. The second statement is indirectly supported by the context. While the context does not explicitly state that Paris has a "rich cultural heritage," it does mention that Paris is known for its culture and history, which can be interpreted as a rich cultural heritage. Verdict: Yes
 3. The third statement is directly supported by the context, which mentions the Eiffel Tower as a landmark in Paris. Verdict: Yes

Retrieval Augmented Generation: Groundedness/Faithfulness

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$$\text{Faithfulness} = 3/3 = 1.0$$

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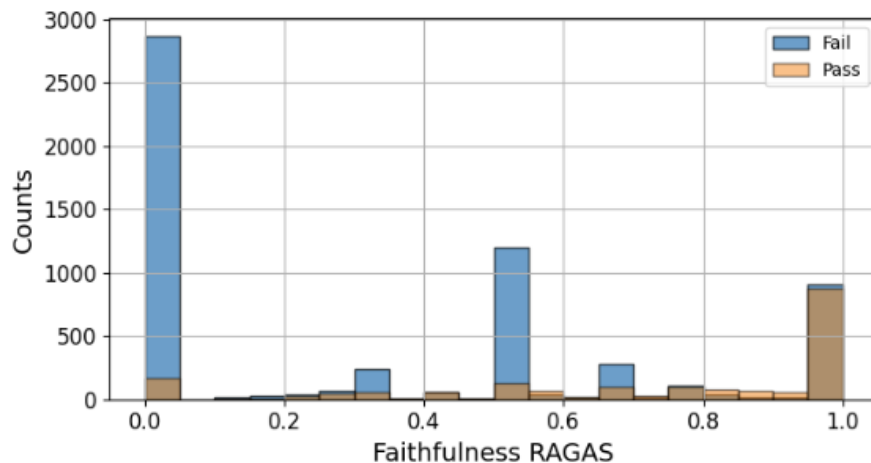
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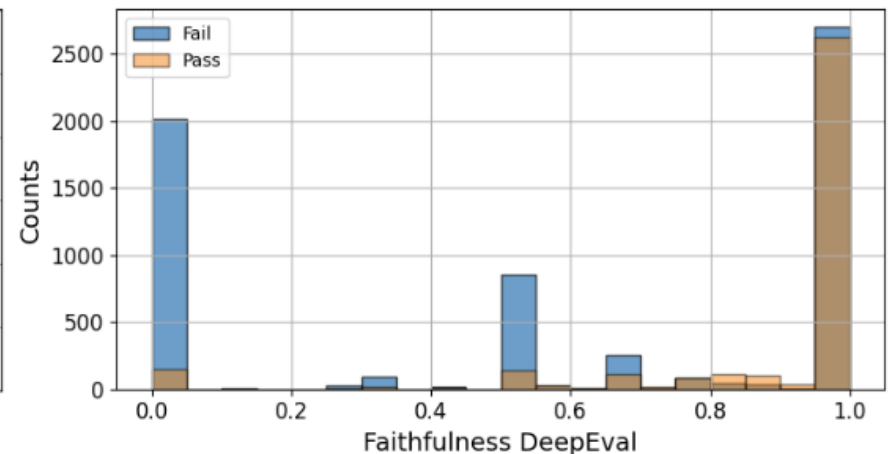
Retrieval Augmented Generation: How to set thresholds ...



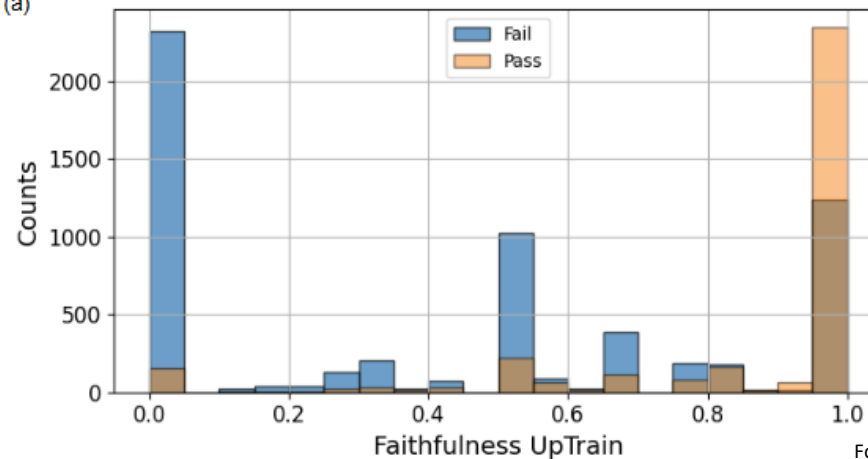
- Dataset: HaluBench is a publicly available dataset with 15k samples each with Context-Question-Answer triplets, and human annotation Hallucinated (Fail)/Not Hallucinated (PASS).
- Run the RAGAS, DeepEval and UpTrain Faithfulness computations, for example, and we get the following distribution (for 9616 samples – after data cleaning).



(a)



(b)



(c)

Retrieval Augmented Generation: How to identify thresholds ...

Step-1A: Identify risks of the specific application and a specific evaluation metric that can quantify the risks.

- There may be multiple risks for the business unit for a given AI application; Legal/compliance/regulatory, reputational, financial, etc.;
- E.g., The chatbot might generate answers not supported by the retrieved documents;
 - Potential dissemination of outdated or incorrect financial data.
- Essentially, prescribe a methodology to assign a risk rating for each AI application.
- Then, identify specific evaluation metric(s) to measure the attributes to quantify the risks. E.g., for hallucination related risks, a possible evaluation metric may be Faithfulness.

Step-1B: Identify risk tolerance of the stakeholder(s)

- Identify the risk tolerance of the stakeholder(s) for the specific application by using methods potentially inspired by methods to identify financial risk tolerance.
- **PS:** An academically sound and rigorous way to identify the risk tolerance of the individuals is well-discussed in the Prospect Theory in the Behavioral Economics areas (Kahneman and Tversky, 1979). It can be extended to identify risk tolerance towards AI applications, but research is still underway.
- Say, High/Moderate/Low Risk Appetite.
- Also find trade-off between LLM evaluation cost vs risk.

Step-1C: Map the risk tolerance of the stakeholder(s) to a confidence level.

- The final goal of this exercises is to provide an answer to the following question:

What percentage of Type I (false positive) and Type II(false negative) errors the stakeholder is willing to take for the specific application with respect to the chosen metric?

- To feed a concrete statistic into the downstream computation, we need a statistical confidence level (e.g., only 5% hallucination is accepted for a specific application for moderate risk tolerance, and hence the required confidence level is 95%).

Retrieval Augmented Generation: Generate Ground Truths

Step-2: Prepare Ground Truth Dataset

- It is crucial for any RAG systems to have some ground truth pairs (Question-Answer) or, even better, triplets (Question-Context-Answer (QCA)) to calibrate the system.
- There are various ways to create such ground truth datasets:
 - Manual creation and labeling
 - Synthetic (using another LLM) generation of QCA and manual labeling
- Generate QCA from diverse set of documents (e.g., out of 10K available documents, randomly pick a few 100s and generate QCAs);
- Generate diverse types questions (around 50 different types of questions classified in the computational linguistics literature, e.g., abbreviation, entity, description, human, location, numeric, etc.);
- Generate questions from different possible topics from the documents (e.g., first perform topic modeling on all the available documents in the training set using say BERT topic modeling or else, and then generate a few QCA from each of the topics);
- Generate questions such that the context is insufficient to provide answers, so that the ground truth dataset also has enough 'negative' examples.

Step-3: Determine the Threshold for the Metric and Cross-Validate

- E.g., compute Faithfulness for the risk of hallucination for the available QCA triplets in the ground truth data.
- Compute mean (say, μ_F and μ_{AR}) and standard deviation (say, σ_F and σ_{AR}) for each of them.
- Compute the confidence intervals. **Confidence Level** represents the degree of certainty that the AI system's performance will meet or exceed the threshold.

CI for Faithfulness: $\mu_F \pm (\text{Z-score for given \% confidence}) \sigma_F$

CI for Answer Relevance: $\mu_{AR} \pm (\text{Z-score for given \% confidence}) \sigma_{AR}$

E.g. (completely hypothetical),

- **High Risk Appetite: 90% Confidence Level:** Willing to accept that in 10% of cases, performance may fall below the threshold.
- **Moderate Risk Appetite: 95% Confidence Level:** Accepts only a 5% chance of performance falling below the threshold.
- **Low Risk Appetite: 98-99% Confidence Level:** Aims for performance to meet thresholds in 98-99% of cases, allowing only 1-2% chance of falling below.

Retrieval Augmented Generation: How to identify thresholds ...

Step-3: Compute the threshold for the given risk appetite

- E.g., for moderate risk appetite

$$\begin{array}{lll} \text{Threshold Faithfulness} & = & \mu_F - (\text{Z-score for 95\% confidence}) \sigma_F \\ \text{Threshold for Answer Relevance} & = & \mu_{AR} - (\text{Z-score for 95\% confidence}) \sigma_{AR} \end{array}$$

Retrieval Augmented Generation: How to identify thresholds ...

Even better... identify the threshold using cross-validations:

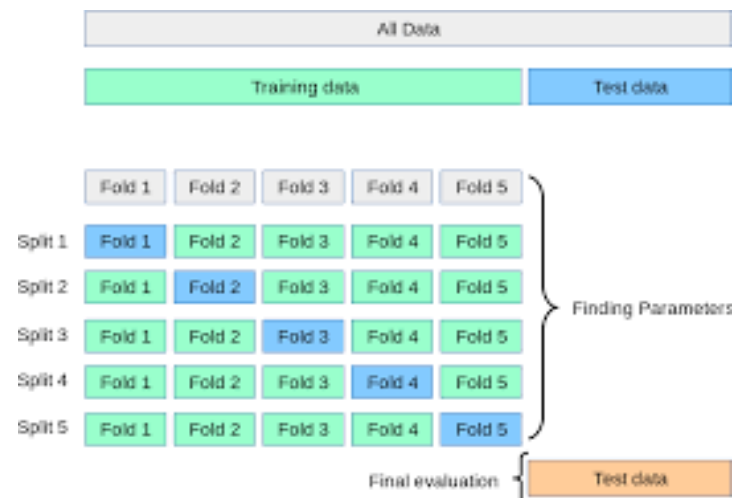
Step 1: Identify and quantify the relevant risks and risk appetite (e.g., 95% confidence level);

Step 2: Run the RAG system to generate outputs for the ground truth data, and calculate the evaluation scores.

Step 3: Take K-folds, and calculate statistical measures (mean, standard deviation) for K-1 folds, compute the threshold using $\mu - Z \times \sigma$.

Step 4: Check how the threshold did on the hold-out fold.

Step 5: Take an average of the thresholds (or the largest value) as the final threshold.



Retrieval Augmented Generation: How to identify thresholds ...

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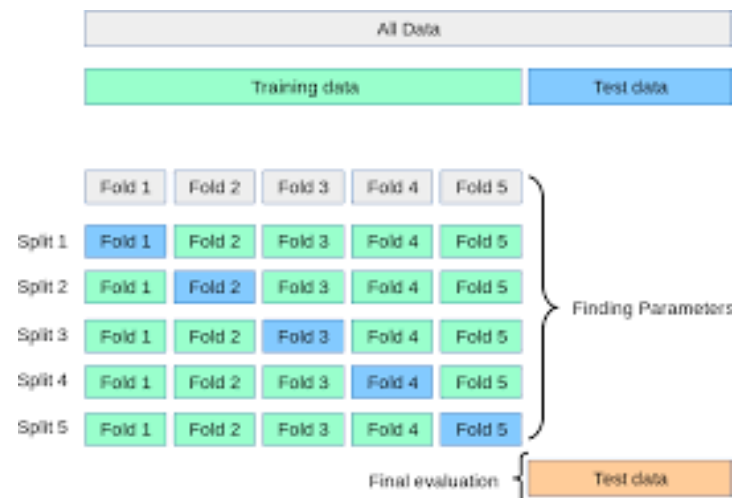
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Even better, other statistical methods such as conformal prediction that does not assume normal distribution etc.

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Other statistical methods for choosing thresholds

- Kernel Density Estimation to identify the 'mid-point' between the distributions of Pass and Fail labels;
- Compute AUC-ROC for a logistic regression between the faithfulness score as the input and the ground truth labels as the output, and pick the threshold as per the probability threshold;
- Instead of logistic regression, use a nonlinear model such as polynomial logistic regression or Generalized Additive Models (GAMs);
- Conformal prediction – distribution free, model agnostic choice methods to pick a threshold for a given confidence level;
- Etc.

Example Thresholds for Faithfulness on the HaluBench data

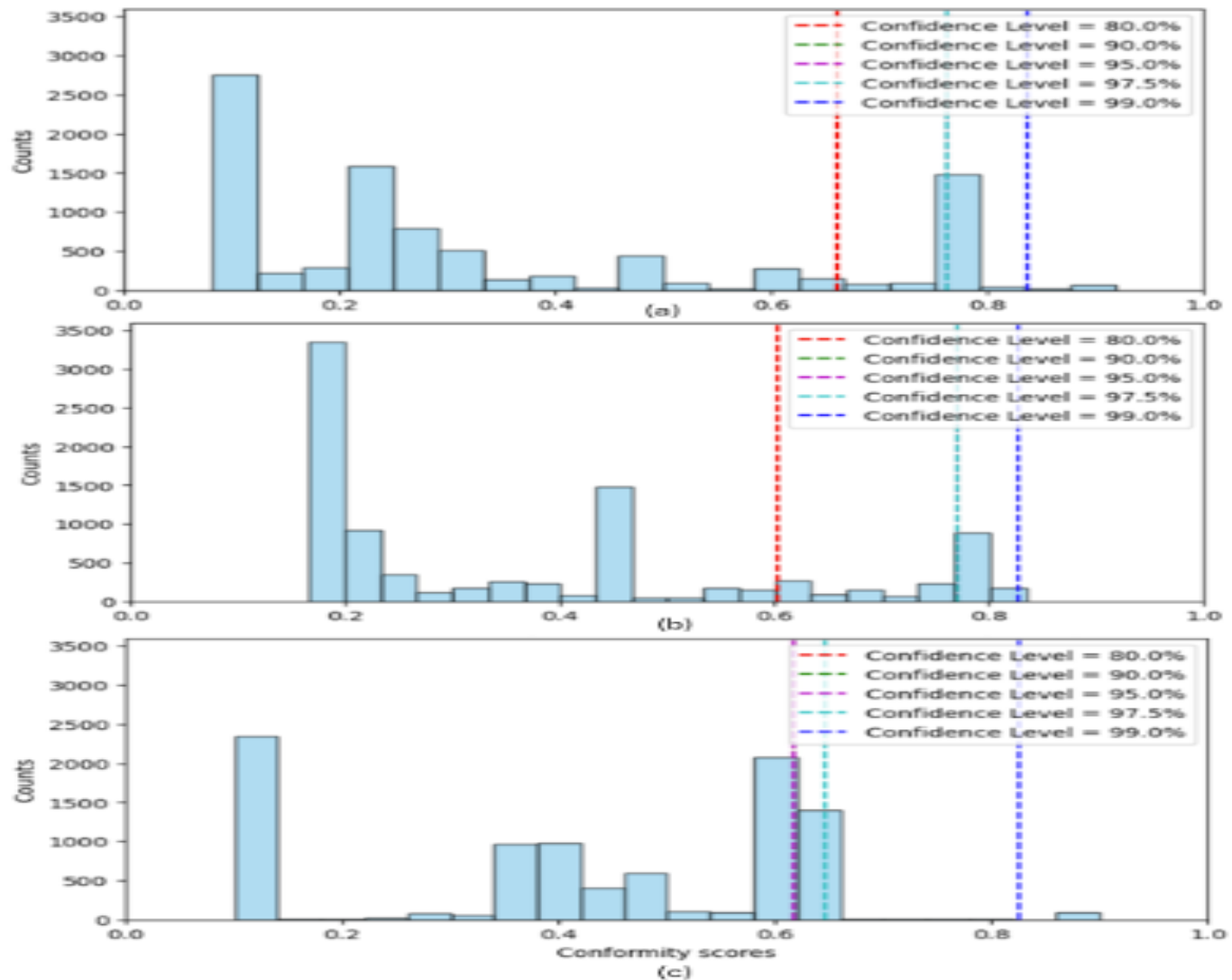
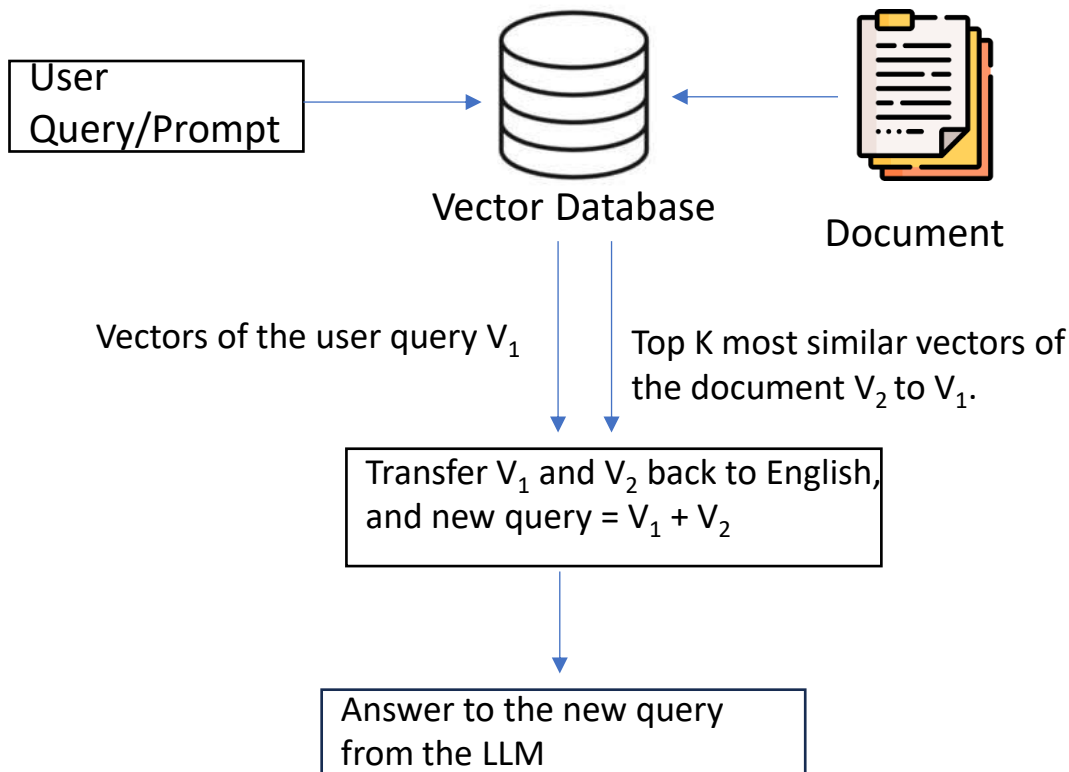


Figure 8: Distribution of conformity scores with thresholds. (a) UpTrain, (b) RAGAS, (c) DeepEval.

Conclusion

- Identifying threshold of an LLM evaluation metric is an immediate problem to be solved when developers need to deploy LLM applications;
- We provide a systematic process to determine the threshold based on risks of the application and risk appetite of the stakeholders;
- We also proposed various statistical methods to compute the threshold in practice;
- Applied these methods on a publicly available dataset for hallucination benchmark for the faithfulness metric.
- Future work: tackling multiple evaluation metrics and their threshold simultaneously.

An Application: Retrieval Augmented Generation



- Get embedding vectors for the user query from a language model (also called vector database).
- Get the embedding vectors for the concerned document(s) from the same vector database.
- PS: This language model can be any model, including TFIDF/BERT/GPT etc.
- Then, identify the K most similar vectors from the set of vectors of the documents.
- Now take convert both sets of vectors back to the language, i.e., 'augment' the original query with the 'context' text from the document, i.e.,
new query = query + context.
- Get the answer from the LLM for 'new query'.